

You must show your work to get full credit.

Let $P(t)$ be defined by the initial value problem

$$\frac{dP}{dt} = -.2P + 400, \quad P(0) = 2,000$$

1. Give a formula for $P(t)$.

The eqn is when $-.2P + 400 = 0$ $P(t) = \underline{2000}$

$$P = \frac{400}{.2} = 2000$$

Let $y = P - 2000$, so $P = y + 2000$

$$P' = y' = -.2(y + 2000) + 400 = -.2y$$

$$y = y(0)e^{-.2t}$$

so $P = y(0)e^{-.2t} + 2000$

$\rightarrow P(0) = 2000$
 $y(0) = 0$

2. What is $P(3)$?

$$P(3) = \underline{2000}$$

3. Estimate $P(100)$.

$$P(100) \approx \underline{2000}$$